Pacing Guide Page 1 of 1

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4/8/20: Topic 1 SAS 1 and SAS 2 #1
4/9/20: Topic 1 SAS 2 #'s 2 – 5 and SAS 3
4/10/20: Topic 2 SAS 2
4/13/20: Topic 2 SAS 4
4/14/20: Topic 3 SAS 2
4/15/20: Topic 3 SAS 3 and SAS 4
4/16/20: Topic 4 SAS 1 and SAS 2
4/17/20: Topic 4 SAS 4 and Topic 5 SAS 4
4/20/20: Topic 6 SAS 2 #'s 1 - 5
4/21/20: Topic 6 SAS 2 #6 and SAS 3
4/22/20: Topic 6 SAS 4
4/23/20: Topic 6 SAS 5
4/24/20: Topic 7 SAS 1
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Support for students, parents, and guardians:

- Teachers will be available to answer questions through Zoom on the following dates. To access the support call, follow the directions below:
 - April 14th, 12:00 p.m. 12:45 p.m.
 - Click on the link: https://zoom.us/j/3791568353
 - Open Zoom app, click join, and enter Meeting ID: 379 156 8353
 - April 21st, 12:00 p.m. 12:45 p.m.
 - Click on the link: https://zoom.us/j/3791568353
 - Open Zoom app, click join, and enter Meeting ID: 379 156 8353



Topic 1: Arithmetic and geometric sequences and series Student Activity Sheet 1; *Overview*

Page 1 of 2

REVIEW What are some key characteristics of linear, quadratic, and exponential
functions? When considering each function, consider their respective graphical
characteristics and the specific characteristics of the equations that describe each
function.

REINFORCE Capture your understanding of arithmetic and geometric sequences by completing this table. State the ideas in your own words and provide your own examples, but also try to incorporate mathematical terms like common difference and common ratio.

Geometric sequence	Arithmetic sequence	Vocabulary term
		What the term means
		An example



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Topic 1: Arithmetic and geometric sequences and series Student Activity Sheet 1; *Overview*

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- REINFORCE Identify each pattern as an arithmetic sequence, geometric sequence, or neither type of sequence. Identify the common difference and common ratio, when necessary.
- a. 10, 18, 26, 34, ...

b.
$$\frac{1}{2}$$
, $\frac{1}{3}$, $\frac{2}{9}$, $\frac{4}{27}$, ...

c. 5, 25, 125, 625, ...

d. 6, 15, 45, 157.5, ...

e. 4, 3.98, 3.96, 3.94, ...



Student:

Topic 1: Arithmetic and geometric sequences and series Student Activity Sheet 2; *Exploring* "Arithmetic sequences and series"

Page 1 of 2

1. REINFORCE Find the first four terms of a sequence using the recursive definition.

$$f(n) = f(n-1) + 2$$
for integer values of $n > 1$

b.
$$f(1) = 10$$

 $f(n) = f(n-1) - 2.5$
for integer values of $n > 1$

c.
$$f(1) = 9$$

 $f(n) = 2f(n-1)$
for integer values of $n > 1$

d.
$$f(1) = 2$$

 $f(n) = -4f(n-2)$
for integer values of $n > 1$

$$f(1) = -6,$$

$$f(1) = 3$$

e.
$$f(0) = -6$$
,
 $f(1) = 3$
 $f(n) = 2f(n-1) + f(n-2)$
for integer values of $n > 2$



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Student: _Class: _Date_

Topic 1: Arithmetic and geometric sequences and series Student Activity Sheet 2; Exploring "Arithmetic sequences and series"

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2. **REINFORCE** Consider the sequence -8, -3, 2, 7, 12, 17.... Write a recursive definition

and a general formula for this sequence.

definition and a general formula for this sequence. 3. REINFORCE Consider the sequence 8, 12, 18, 27, 40.5, 60.75.... Write a recursive

and a general formula for this sequence. 4. REINFORCE Consider the sequence 30, 21, 12, 3, -6, -15.... Write a recursive definition

general formula for this sequence. **5. REINFORCE** Consider the sequence 64, 16, 4, 1, $\frac{1}{4}$, $\frac{1}{16}$... Write a recursive definition and a

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Topic 1: Arithmetic and geometric sequences and series Student Activity Sheet 3; Exploring "Geometric sequences and series"

Page 1 of 4

1. REINFORCE Consider the following geometric series:

256+128+64+32+16+8+4 Using the formula, find the sum of the geometric series.

REINFORCE The drama club is performing a play where they will make \$5000 on the first night.Each night after the first, their revenue will be 85% of the previous night's revenue.

	a)
Night	a) Use this informat
_	nation to estimate t
2	the projected revenue fo
ω	evenue for the fi
4	irst 5 nights of t
ъ	he production.

b) Using the formula, determine the total amount of revenue the drama club will make for their

first 15 performances.

- 3. REINFORCE Traveling carnivals move from town to town, staying for a limited number of days before moving to the next stop. The management of a certain carnival knows that, each time it opens in a new town, it can expect to bring in about \$15,000 in revenue the first night. Each night after the first, revenue will be about 75% of the previous night's revenue. To the nearest dollar, about how much total revenue would the carnival expect after spending two weeks (14 days) in the town?
- **4. REINFORCE** A bookstore chain sold 10,000 copies of a newly published novel in its first month on the shelves. Historically, sales of new novels fall by 20% each month. Which of the following could be used to determine the number of books sold in the first 6 months?

A.
$$S_6 = 10,000 \left(\frac{1 - (0.2)^6}{1 - (0.2)} \right)$$

B.
$$S_6 = 10,000 \left(\frac{1 - (0.8)^6}{1 - (0.8)} \right)$$

C.
$$S_{24} = 10,000 \left(\frac{1 - (0.8)^{24}}{1 - (0.8)} \right)$$

D.
$$S_{24} = 10,000 \left(\frac{1 - (0.2)^{24}}{1 - (0.2)} \right)$$

E.
$$S_6 = 10,000 \left(\frac{1 - (0.8)^6}{1 - (0.2)} \right)$$

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Topic 2: Understanding inverse relationsStudent Activity Sheet 2; Exploring "The inverse of a linear function"

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REINFORCE The CBA Credit Union offers a cash-back checking account that rewards a
member with a \$0.07 deposit to a linked savings account every time the member uses the
CBA debit card to make a purchase. New members also receive a \$4 cash-back reward
bonus when they set up these accounts.

Suppose you become a member of this credit union and sign up for the cash-back checking account. Write a function that shows the relationship between the total number of debit card purchases you have made, p, and the total amount of cash-back rewards you have received, c.

- REINFORCE Use the function rule from the previous question to determine your total cash-back rewards after making 30 debit card purchases.
- REINFORCE Using the same function rule, how many debit card purchases would you have to make to earn a total of \$40 in cash-back rewards?
- 4. **REINFORCE** Find the inverse function of y = 3x 15.
- **REINFORCE** Graph the inverse function of f(x) = 4x + 2.



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Topic 2: Understanding inverse relations Student Activity Sheet 2; Exploring "The inverse of a linear function"

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- 6. REINFORCE For each of the following function rules, generate a table of data describing the function, f, and its inverse, g. Then, generate the rule for the inverse in two ways: directly from the data for the inverse and by algebraic manipulation of the original function rule. If necessary, show that your two inverse rules are equivalent.
- a. f(x) = 100 + 4x

50	25	0	-25	-50	×	
					f(x)	
					×	

			X
			g(x)

b.
$$f(x) = -\frac{1}{4}x + 100$$

			<u>×</u>	
			X	
			g(x	

100

0

400 100 200 300

c.
$$f(x) = \frac{x+25}{5}$$
 (Choose your own set of x-values.)

		X
		$(x)_{\mathcal{J}}$
		g(x)



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Topic 2: Understanding inverse relations Student Activity Sheet 2; *Exploring* "The inverse of a linear function"

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7. **REINFORCE** Find the inverse function of y = -3x + 8.

8. **REINFORCE** Find the inverse function of $y = \frac{3}{5}x - 12$.

Student: _Class:

Topic 2: Understanding inverse relations Student Activity Sheet *4*; Exploring "The quadratic function and its inverse"

Page 1 of 3

1. REINFORCE Could a quadratic function model the data in the table below? Justify your

2	1	0	-1	-2	х
9	2	-1	0	5	У

f(x) and its inverse, $f^{-1}(x)$. Sketch a graph of f(x) and $f^{-1}(x)$ on the same graph grid. Is the **2. REINFORCE** Consider the function $f(x) = x^2 - 8$. Fill in the following tables to describe inverse relation a function? Explain.

-10			
0	10	20	
1 0			
20			
	0	0 10	0 10

		ì
		f(x)
		×
		$f^{-1}(x)$



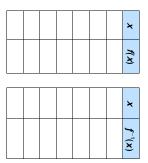
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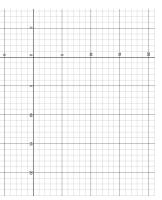
Student: _Date_

Topic 2: Understanding inverse relations Student Activity Sheet *4*; Exploring "The quadratic function and its inverse"

Page 2 of 3

3. Reinforce Consider the function $f(x) = -2x^2 + 18$. Fill in the following tables to describe f(x) and its inverse, $f^{-1}(x)$. Sketch a graph of f(x) and $f^{-1}(x)$ on the same graph grid. Is the inverse relation a function? Explain.





the inverse relation a function? Explain. **4. REINFORCE** Consider the function $f(x) = \sqrt{x-4}$. Fill in the following tables to describe $f(\mathbf{x})$ and its inverse, $f^{-1}(\mathbf{x})$. Sketch a graph of $f(\mathbf{x})$ and $f^{-1}(\mathbf{x})$ on the same graph grid. Is

					3
					×
					$f^{-1}(x)$
					()
					3
		8	8	20	8
-	•	8	- 8	8	-
					-
					E
8					F
					E
5					
8					E
-50					
- 20					E
8					
- 8					



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c 2: Understanding inverse relations int Activity Sheet 4; Exploring "The quadratic function and its inverse" Page 3 of 3
INFORCE Restrict the domain of $f(x)$ to the largest possible set of values such that the se of f is a function. Find an algebraic rule for $f^{-1}(x)$, the inverse of f .

- Topic Student Studer Studer inverse
- a. $f(x) = 4x^2$
- b. $f(x) = x^2 + 3$
- c. $f(x) = x^2 5$
- **6. REINFORCE** Is the inverse of $y = x^4$ a function? Justify your answer.

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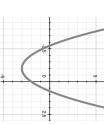
Topic 3: Transforming functionsStudent Activity Sheet 2; Exploring "Transformations to fit data"

Page 1 of 2

1. **REINFORCE** Graph the function $f(x) = (x - 4)^2$. How does this graph compare to the graph of the parent function $y = x^2$?



- 2. How do the parameters a, h, and k in the general equation $y = a(x h)^2 + k$ affect the graph of a quadratic function?
- 3. **REINFORCE** For each graph, write the equation of the quadratic function in vertex form: $y = a(x - h)^2 + k$. Also describe the transformation from the parent function $y = x^2$.





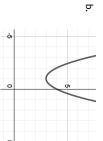
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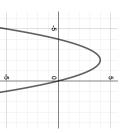
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Topic 3: Transforming functionsStudent Activity Sheet 2; Exploring "Transformations to fit data"





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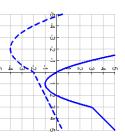


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Topic 3: Transforming functionsStudent Activity Sheet 3; Exploring "Generalizing transformations"

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1. REINFORCE The graph of the parent function rule f(x) (the solid blue line) has been transformed to create the graph of a new function rule af(x-h)+k (the dashed blue line). Using the answer choices provided, fill in the blanks to complete true statements about the values of a, h, and k.



left	wider
right	narrower
negative	a > 1
positive	a is negative
up	0 < <i>a</i> < 1
down	<i>a</i> > 1

a: T
The
The transformed func
function
graph
S
than
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graph, so
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transformed function graph is shifted to the	
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$$k$$
: The transformed function graph is shifted ______, so k is ______



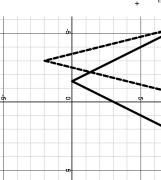
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Student Activity Sheet 3; Exploring "Generalizing transformations" Page 2 of 4

create the graph of a new function rule af(x - h) + k, the dashed line. Using the answer choices provided, fill in the blanks to complete true **REINFORCE** The graph of the parent function rule g(x), the solid line, has been transformed to statements about the values a, h, and k.



a: The trans	left	wider
a: The transformed function graph is	right	narrower
graph is	negative	a > 1
than the orig	positive	<i>a</i> is negative 0 < <i>a</i> < 1
than the original graph, so	qp	0 < <i>a</i> < 1
	down	<i>a</i> > 1

 $\emph{\textbf{k}}$: The transformed function graph is shifted

_, so *k* is

so h is

h: The transformed function graph is shifted to the

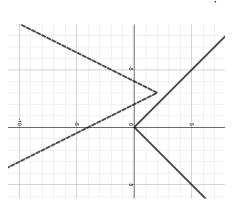
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Topic 3: Transforming functionsStudent Activity Sheet 3; Exploring "Generalizing transformations"

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3. **REINFORCE** What values of a, h, and k will transform the graph of the original function, f(x), shown with the solid line, so that it matches the graph of the new function rule y = af(x - h) + k, the dashed line?

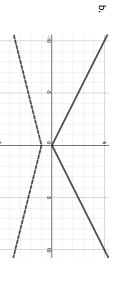


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Topic 3: Transforming functionsStudent Activity Sheet 3; Exploring "Generalizing transformations"

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Student: _Class:_

Topic 3: Transforming functionsStudent Activity Sheet 4; Exploring "Making the algebra-geometry connection"

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1. **REINFORCE** Write g(x) in terms of f.

	X	f(x)
٨	÷۵	-12
В	-1	2
С	0	3
D	2	-7

ō	C'	B'	Α'	
ر ت	3	2	0	Х
ယ်	7	6	-8	g(x)

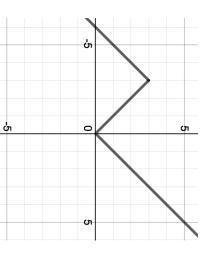
2. **REINFORCE** How is the graph of g(x) related to the graph of f(x) if g(x) = f(x + 7) - 3?

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Topic 3: Transforming functionsStudent Activity Sheet 4; Exploring "Making the algebra-geometry connection" Student: _Class: _Date_

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3. **REINFORCE** Given the following graph of the function f(x), sketch and label the graphs of g(x) = f(x-4) and h(x) = f(x+3)



4. **REINFORCE** The function h(x) is defined as $h(x) = \frac{1}{3}f(x-2) + 4$. Describe the compressions or stretches. relationship between h(x) and f(x) in terms of horizontal and vertical shifts and vertical

Topic 4: Introduction to polynomial functions Student Activity Sheet 1; Overview Student: _Date_ Page 1 of 4

1. **REVIEW** Simplify each expression.

a.
$$5x^2 + 4x - 2xy - 5x - 2x^2 + 4xy + y^2$$

b. $x(7 - 3x) - 2(2x^2 + 3x) + 12$

c. (x-5)(x+2)

d.
$$(3x + 7)(2x - 3)$$

Student: _Date_

Topic 4: Introduction to polynomial functions Student Activity Sheet 2; Exploring "Building polynomials"

Page 2 of 4

- 1. REINFORCE Find the indicated sum or difference.
- a. (x-1) + (5x+10) (2-3x)

b.
$$(x^3 - 4x^2 + 2x - 3) + (8 - 2x^2 + x)$$

c. $(5x - 3x^2) - (4 - 2x^2)$



- 2. **REINFORCE** Find the indicated products.
- a. (x+4)(x-3)
- b. $(x^2 9)(x 2)$
- c. (x+2)(x-2)(x+5)
- d. (x+1)(x-3)(x+2)



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Tonic 1: Introduction to polynomial functions	
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1	Student: Class: Date
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oduction to polynomial functions y Sheet 2; Exploring "Building polynomials"

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- 3. REINFORCE A rectangular cooler is 12 inches long, 9 inches wide, and 9 inches deep.
- a. What is the volume of the cooler?
- b. If each dimension is increased by $oldsymbol{x}$ inches, what would be the new volume?

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Topic 4: Introduction to polynomial functionsStudent Activity Sheet 4; Exploring "Deepening your understanding of quadratics and cubics"

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1. **REINFORCE** For the function $f(x) = x^2 + 2x + 4$, find the average rate of change for the intervals $1 \le x \le 3$ and $3 \le x \le 7$.

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Topic 5: Analyzing polynomial functions Student Activity Sheet 4; *Exploring* "Higher degree polynomials"

Page 2 of 2

- 1. REINFORCE How many \boldsymbol{x} intercepts do the graphs of the following functions have? What are they?
- a. $f(x) = x^3 + x$
- b. $g(x) = (x+1)(x-1)^2$
- c. $h(x) = x^3 + 27$
- d. $j(x) = x^3 1$



Student:Class:	Date	Student:
Topic 6: Polynomial equations Student Activity Sheet 2; Exploring "Quadratic equations"	Page 1 of 4	Topic 6: Polynomial equations Student Activity Sheet 2; Exploring "Qu

1. REINFORCE A Roman candle firework is launched from a platform 8 feet above the ground. The firework has an initial velocity of 150 feet per second. A function that models the firework's vertical distance with respect to time, t, is $h(t) = -16t^2 + 150t + 8$

Approximately when will the firework hit the ground?

the function $h(t) = -16t^2 + 32$. How long will it take for the tomato to hit the ground? 2. REINFORCE The height of a tomato dropped from 32 feet above the ground is given by

3. REINFORCE Solve each of the following quadratic equations using factoring, when

a.
$$4x^2 - 16x = -16$$

possible.

b.
$$x^2 - 9 = 0$$

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Student Activity Sheet 2; Exploring "Quadratic equations"

Page 2 of 4

c.
$$x^2 - 10x + 25 = 0$$

d.
$$x^2 = 12x$$

4. REVIEW Sketch three parabolas that illustrate the different possibilities for the x-intercepts of the graph of a quadratic function.



Student:Class:Date	<u>'</u>
Topic 6: Polynomial equations Student Activity Sheet 2; Exploring "Quadratic equations" Page 3 of 4	Topic 6: Polynomial equations Student Activity Sheet 2; Exploring "Quadratic equations"

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- 5. REVIEW SO ratic formula.
- **a.** $2x^2 4x 2 = 0$

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é
each
앜
the
following
-0
luadratic
olve each of the following quadratic equations using the quad
using
the
quad

ŗ
$5x^2$
1
2x
1
9
Ш
0

as possible. Classify the roots as two real roots, one real root, or two non-real complex roots. Then use your graphing calculator to compare each equation to the graph of its 6. REINFORCE Solve each of the following quadratic equations, simplifying answers as much related function. student Activity sneet 2; Exploring "Quadratic equations" **b.** $3x^2 + 45 = 0$ a. $2x^2 - 3x = -11$ Page 4 of 4



C. $-4x^2 = -3x + 15$

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Student:

Topic 6: Polynomial equations Student Activity Sheet 3; *Exploring* "Complex numbers"

Page 1 of 2

- 1. **REVIEW** Rewrite each imaginary number in terms of i.
- a. $\sqrt{-16}$
- $b.\sqrt{-24}$
- 2. **REINFORCE** Calculate each power of i.
- a. /8 =
- b. /²66 = __
- c. $b^{33} =$ ____
- 3. **REINFORCE** Compute each of the following sums and differences.
- a. (3 + 4i) + (1 2i)
- b. (-4 + 8i) (2 + 18i)
- 4. **REINFORCE** Compute each of the following products.
- a. (3 + 4i)(1 2i)
- b. (-4 + 12i)(2 + 12i)

Topic 6: Polynomial equations Student Activity Sheet 4; Exploring "Other polynomial equations"

Class:

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Page 2 of 2

1. REINFORCE Rewrite each expression in factored form.

a.
$$5x^3 + 10x^2 + 15x + 30$$

b.
$$x^3 + 3x^2 + 4x + 12$$

<u>.</u> $27x^3 + 64$

d. χ⁶ - y⁶

e. $6x^4 - 28x^3 - 25x^2 + 70x + 25$

f. $4x^3 + 12x^2 - 25x - 75$



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Topic 6: Polynomial equations Student Activity Sheet 5; *Exploring* "Theorems of algebra"

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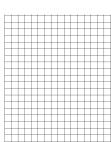
1. REINFORCE Solve each of the cubic equations in question 1 over the complex numbers. a. $x^3 + 4x^2 - 11x - 30 = 0$



b.
$$x^3 + 4x^2 - 11x + 6 = 0$$



c.
$$x^3 + 4x^2 - 10x + 12 = 0$$





Topic 6: Polynomial equations
Student Activity Sheet 5; Exploring "Theorems of algebra" 2. For $p(x) = x^3 + 3x^2 - 6x - 8$, find the remainder upon division for the given factor and evaluate the function for the given point. Student: *p*(*x*) *p*(x) _Class: _Date_

Topic 6: Polynomial equations
Student Activity Sheet 5; Exploring "Theorems of algebra"

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3. Using synthetic division, find the quotient of the following:

4. The cubic polynomial $2x^3-x^2-25x-12$ has one linear factor (2x+1). What are the other linear factors?

Student: _Date_

Topic 7: Exponents and radicals Student Activity Sheet 1; *Overview*

Page 1 of 2

REINFORCE Simplify each numerical expression using the laws of exponents. Leave your answers in exponential form.

b.
$$2^{-4} \cdot 3^6 \cdot 2^8 =$$

C.
$$\frac{a^9}{a^{-3}} =$$

$$\cdot \frac{2b^3}{c^6} \cdot \left(\frac{2^2b^{-4}}{c^2}\right)^{-2}$$

$$\mathbf{e.} \ \frac{16a^4b^{-5}}{c^2} \cdot \frac{a^7b^3}{4c} = \underline{\hspace{1cm}}$$

f.
$$(3a^{-3}b^6)^4 =$$



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Student: _Date_

Topic 7: Exponents and radicals Student Activity Sheet 1; *Overview*

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- 2. REINFORCE Create expressions that meet the conditions specified
- a. The expression simplifies to 4^2x^4y using the multiplication rule.

b. The expression simplifies to $\frac{5x^7}{y^3}$ using the division rule, and has at least one negative exponent.

c. The expression simplifies to $5^3 \mathbf{x}^5 \mathbf{y}^2$ using the multiplication rule and the power rule, and has at least two negative exponents.

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Algebra II Answer Sheet

4/8/20:

Topic 1 Student Activity Sheet 1 Linear Graph is a straight line

Equation is y = x

Graph is a parabola Equation is $y = x^2$

a. Graph increases rapidly from a small value as it moves to the right or decreases rapidly from a large value as it moves to the right b. There are many different examples of exponential equations. There must be a base value with a variable exponent: $y = 2^x$, $y = 3^x$, $y = \left(\frac{1}{2}\right)^x$, etc.

		2.
Geometric sequence	Arithmetic sequence	Vocabulary term
Sequence created by multiplying a specific value to each term to create the next term. The number that is multiplied to each term to get the next term is called the common ratio	Sequence created by adding or subtracting a specific value to each term to create the next term. The number that is added to each term to get the next term is called the common difference.	What the term means
There are many examples of geometric sequences, just make sure the sequence follows a pattern of multiplying by the same value: • $r = \frac{2}{2}$ • 4 , 2 , 1 , $\frac{1}{2}$, $\frac{1}{4}$ $r = \frac{1}{2}$	There are many examples of arithmetic sequences, just make sure the sequence follows a pattern of adding or subtracting the same value: 5, 7, 9, 11, 13 4 = 2 9, 4, 11, -6, -11 d = -2 d d = 2 1 d d = 2 1 d d = 10	An example

- 3. a. Arithmetic Sequence d = 8
- b. Geometric Sequence $r = \frac{2}{3}$
- c. Geometric Sequence r = 5
- d. Neither Arithmetic or Geometric
- e. Arithmetic Sequence d = -0.02



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Algebra II Answer Sheet

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Topic 1 Student Activity Sheet 2 # 1

1. a. 4, 6, 8, 10 b. 10, 7.5, 5, 2.5 c. 9, 18, 36, 72 d. 2, -8, 32, -128 e. -6, 3, 0, 3

4/9/20:

Topic 1 Student Activity Sheet 2#'s 2-52. Recursive: f(n) = f(n-1) + 5

General Formula: $a_n = -8 + 5(n-1)$

- 3. Recursive: f(n) = 1.5f(n-1)
- General Formula: $a_n = 8(1.5)^{n-1}$
- 4. Recursive: f(n) = f(n-1) 9
- General Formula: $a_n = 30 9(n 1)$
- 5. Recursive: $f(n) = \frac{1}{4}f(n-1)$
- General Formula: $a_n = 64 \left(\frac{1}{4}\right)^{n-1}$

1.508 Topic 1 Student Activity Sheet 3

2. a.					
Night	1	2	3	4	5
Revenue \$5	\$5000	\$4250	\$3612.50	\$3070.63	\$2610.03
b. \$30,421.53					

- 3. \$58,930.92
- 4. B



$\frac{4/10/20:}{\text{Topic 2 Student Activity Sheet 2}}$ 1. c = .07p + 4

- 3. p = 5152. c = \$6.10
- 4. $y^{-1} = \frac{1}{3}x + 5$
- 5. $f^{-1}(x) = \frac{x-2}{4}$

ba.				
X	F(x)	X	G(x)	
-50	-100	-100	-50	
-25	0	0	-25	
0	100	100	0	
25	200	200	25	
50	300	300	50	

56.			
X	F(x)	Х	G(x)
-100	125	125	-100
0	100	100	0
100	75	75	100
200	50	50	200
300	25	25	300
400	0	0	400

300	23	23	200
400	0	0	400
č.			
X	F(X)	3(X)
0	5		25
1	5.2		-20
2	5.4		-15

,	$7.v^{-1}$
ω	= -x+8

5.6

-10

$$8. y^{-1} = \frac{5}{3}x + 20$$



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Algebra II Answer Sheet

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Topic 2 Student Activity Sheet 4

1. Yes, the second differences are constant.

2.
$$f^{-1}(x) = \sqrt{x+8}$$

2	_	0	-1	-2	X	3.
14	16	18	16	14	F(x)	
	16				Х	
2	1	0	-1	-2	$f^{-1}(x)$	

+			
X	F(x)	X	$f^{-1}(x)$
4	0	0	4
5	1	1	5
8	2	2	8
13	3	3	13
20	4	4	20
29	5	5	29

6.
$$f^{-1}(x) = \sqrt{x-3}$$

7.
$$f^{-1}(x) = \sqrt{x+5}$$

8. No, $y = x^4$ is not a one-to-one function.



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4/14/20:

Topic 3 Student Activity Sheet 2 1. Transforms 4 units to the right.

- a: Vertical Stretch or compression
 h: Horizontal Shift
 k: Vertical Shift
- $\dot{\omega}$
- a. 2 units left and 3 units down.b. 1 unit left and 3 units up.c. Reflects across the x-axis. Shifts 2 units left and 4 units up

4/15/20:

Topic 3 Student Activity Sheet 3 1. a: wider, |a| > 1

- h: Left, Positive k: Down, Negative
- a: Skinnier, 0 < a < 1h: Left, Positive
- k: Down, Negative
- ω a. y = |x + 3| + 2b. y = -|x| - 1

Topic 3 Student Activity Sheet 4 1. g(x) = f(x-3) + 4

- Left 7 and down 3
- 3. g(x) = f(x) shifted right 4 units h(x) = f(x) shifted left 3 units
- 4. Vertical compression of $\frac{1}{3}$. Shifted right 2 units and up 4 units.



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4/16/20:

Topic 4 Student Activity Sheet 1 1. $3x^2 - x + 2xy + y^2$

1.
$$3x^2 - x + 2xy + y^2$$

$$2. -7x^2 + x + 12$$

3.
$$x^2 - 3x - 10$$

4.
$$6x^2 - 5x - 21$$

a.
$$9x + 7$$

b. $x^3 - 6x^2 + 3x + 5$

Topic 4 Student Activity Sheet 2
1. a.
$$9x + 7$$

b. $x^3 - 6x^2 + 3x + 5$
c. $-x^2 + 5x - 4$

a.
$$-x^{2} + x - 12$$

b. $x^{3} - 2x^{2} - 9x + 18$
c. $x^{3} + 5x^{2} - 4x - 20$

2. a.
$$-x^2 + x - 12$$

b. $x^3 - 2x^2 - 9x + 18$
c. $x^3 + 5x^2 - 4x - 20$
d. $x^2 - 7x - 6$

3. a.
$$972 in^3$$

b. $x^3 + 30x^2 + 297x + 972in^3$

4/17/20:

1.6;12 Topic 4 Student Activity Sheet 4

Topic 5 Student Activity Sheet 4

1. a. 1;
$$x = 0$$

b. 2; $x = -1$, 1

c. 1;
$$x = 3$$

d. 1; $x = 1$



Algebra II Answer Sheet

4/20/20:

Topic 6 Student Activity Sheet 2 #'s 1 - 5 1. 9.43 secs

2. 1.41 secs

3. a. x = 2

b. x = -3, 3 c. x = 5 d. x = 0, 12

4. graphs with: no x-intercepts, one x-intercept, and two x-intercepts

5. a.
$$x = 1 \pm \sqrt{2}$$

b. $x = \frac{1 \pm 2\sqrt{46}}{5}$

4/21/20:

Topic 6 Student Activity Sheet 2#'s 6
6. a. $x = \frac{3\pm i\sqrt{79}}{4}$ b. $x = \pm i\sqrt{15}$

c. $x = \frac{3 \pm i\sqrt{231}}{8}$

Topic 6 Student Activity Sheet 3 1. a. $\pm 4i$ b. $\pm 2i\sqrt{6}$ c. $\cdot \pm \frac{3}{5}i$

2. a. 1 b. -1 c. i

3. a. 4 + 2i b. -6 - 10i

4. a. 11 - 2i b. -152 - 24i



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Topic 6 Student Activity Sheet 4 1. a. $5(x^2 + 3)(x + 2)$

b. $(x^2 + 4)(x + 3)$ c. $(3x+4)(9x^2 + 12x + 16)$ d. $(x-y)(x^2 + xy + y^2)(x + y)(x^2 - xy + y^2)$ e. $(x-5)(2x^2 - 5)(3x + 1)$ f. (2x-5)(2x+5)(x+3)

4/23/20:

Fopic 6 Student Activity Sheet 5

1. a. x = -5, -2, 3b. x = -6 and 1 (1 is a solution twice) c. x = -6, 1 + i, 1 - i

2. a. remainder = 0 b. remainder = 28 c. remainder = 0

 $3.2x^3 + 9x^2 + 17x + 42 + \frac{516}{x-3}$

4. (x-4) and (x+3)

4/24/20:

Topic 7 Student Activity Sheet 1
1. a. 7^9 b. $2^4 \cdot 3^6$ c. a^{12} d. $\frac{b^{11}}{2^3c^2}$ d. $\frac{b^{11}}{4a^{11}}$ e. $\frac{b^2c^3}{a^{12}}$ f. $\frac{a^{12}}{a^{12}}$

2. There are a lot of answers that can be correct, but here is one example for each: a. $(4x^3y) \cdot 4x$ b. $\frac{25x^3y^5}{5x^7^4y^6}$ c. $(5^{-2}x^2y^3)^{-2}(5^{-1}x^9y^8)$